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Measurements of the hadronic final state in deeply inelastic ep scattering (DIS) provide precision tests of quantum chromodynamics (QCD). At HERA data are collected over a wide range of the negative four-momentum-transfer Q^2 , the Bjorken variable x and the transverse momenta p_T of hadronic final state objects.

The diagram illustrates a deep inelastic scattering (DIS) process. An incoming lepton L emits a virtual photon γ^* with momentum Q^2 and scatters with momentum q . The virtual photon interacts with a parton x inside a proton p , which then fragments into a hadron \bar{q} . The parton x has momentum $x_g k_f$ and is surrounded by a cloud of gluons represented by wavy lines.

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emitted partons, *i.e.* $k_{t,1} \ll \dots \ll k_{t,n} \ll \dots \ll Q^2$. DGLAP evolution is expected to break down at sufficiently low values of x , when the ordering no longer applies.

At very low values of x it is believed that the theoretically most appropriate description is given by the BFKL evolution equations [2]. These resum large logarithms of $1/x$ up to all orders and impose no restriction on the ordering of the transverse momenta within the parton cascade. Thus off-shell matrix elements have to be used together with an unintegrated gluon distribution function, $f(x, \tilde{\mu}_f^2, k_t)$, which depends on the gluon transverse momentum k_t as well as x and a hard scale $\tilde{\mu}_f$. A promising approach to parton evolution at both low and large values of x is given by the CCFM [3] evolution equation, which, by means of angular-ordered parton emission, is equivalent to the BFKL ansatz for $x \rightarrow 0$, while reproducing the DGLAP equations at large x .

An extended parton ladder at low x leads to high k_t partonic emission in the region close to the proton remnant ('forward' region) to which measurements of jets and leading particles, *e.g.* π^0 are sensitive. Production of a forward π^0 can be regarded as a refined version of forward jet production. In order to enhance the sensitivity to low- x effects special selection cuts have been applied such as confining the ratio $p_{T,(\pi^0, Jet)}^2/Q^2$ to values between 0.5 and 2 inspired by a proposal in [4].

Inclusive forward π^0 cross sections for transverse momenta $p_{T,\pi^0} > 3.5$ GeV are shown in Fig. 2 as a function of x

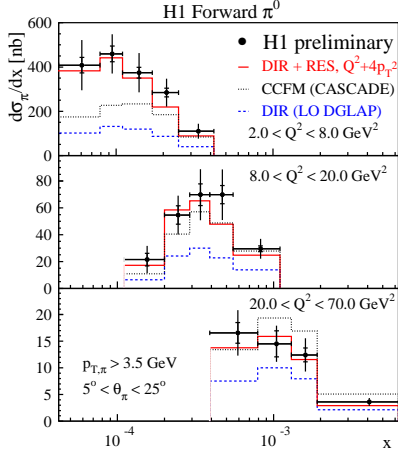


Fig. 2. Forward π^0 cross section as a function of Bjorken- x in different regions of Q^2 compared with predictions of DGLAP and CCFM based QCD Models.

for different regions of Q^2 . The data are compared with predictions of the Monte Carlo models RAPGAP [5] and CASCADE [6]. RAPGAP implements a QCD model based on Leading Order ($O(\alpha_s)$, LO) parton showers with ('DIR + RES') and without ('DIR') resolved photon structure. CASCADE is employed as an implementation of the CCFM evolution equation introduced above. The prediction by RAPGAP with a pointlike photon (DIR) is well below the data. A reasonable description of the data is achieved by including contributions from resolved virtual photons in the predictions and using a factorization scale of $Q^2 + 4p_{T,\pi^0}$. Note, that resolved contributions can be considered to mimic a lack of ordering in transverse momentum as required for a DGLAP evolution scheme. CASCADE predictions based on the unintegrated gluon density JS2001 [6] on the other hand undershoot the data for lower values of Q^2 .

2.2 Forward Jet Cross Sections

Results complementary to the ones discussed in Sec. 2.1 are obtained by studying jets in the same region of phase space. Jets are reconstructed with the longitudinally invariant k_t cluster algorithm [7]. Fig. 3 shows the forward jet cross section for transverse momenta $p_{T,Jet} > 3.5$ GeV as a function of x . The data are compared with NLO ($O(\alpha_s^2)$) QCD calculations performed with the program DISINT [9] and predictions by CASCADE based on two recent sets of unintegrated gluon distributions [8]. While results of the NLO QCD calculations are significantly below the data, the CASCADE prediction based on the set labelled J2003-1 is in good agreement with the data. The difference between the CASCADE predictions indicates the sensitivity of forward jet data to low- x dynamics.

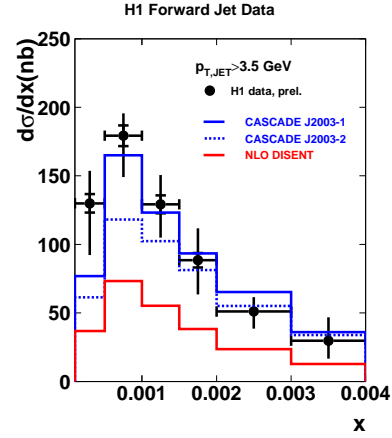


Fig. 3. Forward jet cross section as a function of Bjorken- x compared with NLO DGLAP QCD calculations and predictions by the CCFM Model CASCADE.

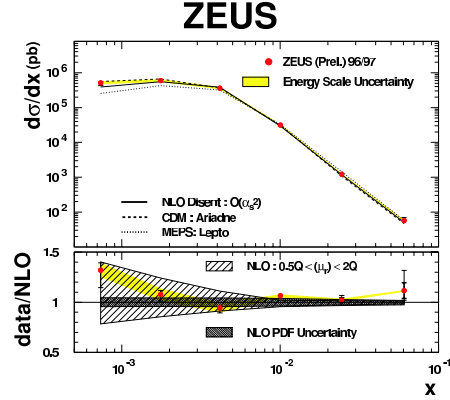


Fig. 4. Inclusive jet cross section as a function of Bjorken- x compared with NLO DGLAP QCD predictions and DGLAP based QCD Models.

3 Inclusive Jet Cross Sections

In the following analysis of inclusive jet cross sections the restriction to the forward region and the kinematic confinement introduced in Sec. 2 are removed, leading to a somewhat more general study of jet cross sections. In [10] it is outlined that the comparison of the measured jet cross sections with matrix element calculations including contributions up to $O(\alpha_s)$ performed with DISINT lead to significant discrepancies between the data and the theoretical predictions. If, however, hadronic activity in the forward and the backward hemisphere is required and NLO ($O(\alpha_s^2)$) predictions are employed a much better agreement between the data and the theoretical prediction is obtained, which is demonstrated in Fig. 4. The theoretical error represented by the hatched band is due to missing higher order contributions in the theoretical calculations. Predictions based on LO DGLAP parton showers, here represented by LEPTO [11], undershoot the data at low- x while a good description of the data is obtained by the CDM [12] model as implemented in the event generator ARIADNE [13].

4 Azimuthal Correlations between Jets

Insight into low- x dynamics can be gained from inclusive dijet data by studying the behavior of events with a small azimuthal separation, $\Delta\phi^*$, between the two hardest jets as measured in the hadronic center-of-mass system [14–16]. Partons entering the hard scattering process with negligible transverse momentum, k_t , as assumed in the DGLAP formalism, lead at leading order to a back-to-back configuration of the two outgoing jets with $\Delta\phi^* = 180^\circ$. Azimuthal jet separations different from 180° occur due to higher order QCD effects. However, in models which predict a significant proportion of partons entering the hard process with large k_t , the number of events with small $\Delta\phi^*$ should also increase.

Here we present a measurement of the ratio

$$S = \frac{\int_0^{120^\circ} N_{\text{dijet}}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}{\int_0^{180^\circ} N_{\text{dijet}}(\Delta\phi^*, x, Q^2) d\Delta\phi^*},$$

of the number of events N_{dijet} with an azimuthal jet separation of $\Delta\phi^* < 120^\circ$ relative to all dijet events. The observable was proposed in [16] and is considered to be directly sensitive to low- x effects.

Fig. 5 presents the S -distribution as a function of x for different Q^2 . It is of the order of 5% and increases with decreasing x . This rise of S is most prominent in the lowest Q^2 bin, where the smallest values of x are reached. The NLO dijet QCD calculations, resulting in an effective LO prediction for S , predict S -values of only $\sim 1\%$ and show no rise towards low x . NLO 3-jet predictions by the program NLOJET [17] which lead to an effective NLO prediction for S give a good description of the data at large Q^2 and large x , but still fail to describe the increase towards low x , particularly in the lowest Q^2 range. According to the discussion given in [18], predictions based on CCFM evolution as implemented in CASCADE lead to an improved overall agreement with the data in particular at low x and Q^2 .

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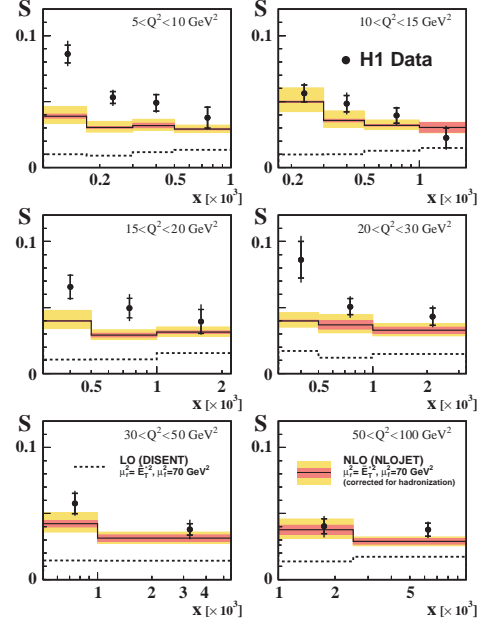


Fig. 5. The observable S given as a function of Bjorken- x and Q^2 compared with LO and NLO DGLAP QCD predictions.

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